

• **A complete example of the simplex method in tabular form**

➤ Consider the LP $\max Z = 3x_1 + 2x_2 + 5x_3$
 s.t. $x_1 + 2x_2 + x_3 \leq 430$
 $3x_1 + \quad + 2x_3 \leq 460$
 $x_1 + 4x_2 \leq 420$
 $x_1 \geq 0, x_2 \geq 0, x_3 \geq 0$

➤ Standard form $\max Z = 3x_1 + 2x_2 + 5x_3$
 s.t. $x_1 + 2x_2 + x_3 + S_1 = 430$
 $3x_1 + \quad + 2x_3 + S_2 = 460$
 $x_1 + 4x_2 + S_3 = 420$
 $x_1 \geq 0, x_2 \geq 0, x_3 \geq 0$

➤ All constraints are “ \leq ” and RHS > 0. Then, the starting solution is O.

↓

| | x_1 | x_2 | x_3 | S_1 | S_2 | S_3 | RHS | Ratio |
|---------|-------|-------|-------|-------|-------|-------|-----|----------|
| Z | -3 | -2 | -5 | 0 | 0 | 0 | 0 | -- |
| S_1 | 1 | 2 | 1 | 1 | 0 | 0 | 430 | 430 |
| ← S_2 | 3 | 0 | (2) | 0 | 1 | 0 | 460 | 230 |
| S_3 | 1 | 4 | 0 | 0 | 0 | 1 | 420 | ∞ |

↓

| | x_1 | x_2 | x_3 | S_1 | S_2 | S_3 | RHS | Ratio |
|---------|-------|-------|-------|-------|-------|-------|------|----------|
| Z | 4.5 | -2 | 0 | 0 | 2.5 | 0 | 1150 | -- |
| ← S_1 | -0.5 | (2) | 0 | 1 | -0.5 | 0 | 200 | 100 |
| x_3 | 1.5 | 0 | 1 | 0 | 0.5 | 0 | 230 | ∞ |
| S_3 | 1 | 4 | 0 | 0 | 0 | 1 | 420 | 105 |

| | x_1 | x_2 | x_3 | S_1 | S_2 | S_3 | RHS |
|-------|-------|-------|-------|-------|-------|-------|------|
| Z | 4 | 0 | 0 | 1 | 2 | 0 | 1350 |
| x_2 | -0.25 | 1 | 0 | 0.5 | -0.25 | 0 | 100 |
| x_3 | 1.5 | 0 | 1 | 0 | 0.5 | 0 | 230 |
| S_3 | 2 | 0 | 0 | -2 | 1 | 1 | 20 |

➤ The optimal solution is $x_1^* = 0, x_2^* = 100, x_3^* = 230$ & $Z^* = 1350$.