

## Chapter 6 Annual Worth Analysis

### • Introduction

- Annual worth (AW) analysis is a variant of the present worth analysis discussed in Chapter 5.
- However, AW analysis has many advantages that make it a useful technique for comparing alternatives.

### • Advantages of AW analysis

- It's a popular analysis technique.
- It's easy to understand. Results are reported in \$/year.
- It simplifies comparing alternatives when cash flows repeat. No need to compare the alternatives over the LCM. Compare over life cycle of each alternative.

### • How does it work?

- For alternative  $j$ , find the uniform annual series, with value  $AW_j$ , which is equivalent to all the cash flows of the alternative at the decision maker's MARR.
- An alternative  $j$  with  $AW_j \geq 0$  is economically viable.
- Compare annualized series (the  $AW_j$ s) of all alternatives
- The alternative with largest  $AW_j$  is selected.
- When cash flows repeat,  $AW_j$  is found over the duration of Alternative  $j$ . No need to compare over the LCM of lives.
- If cash flows don't repeat,  $AW_j$  is found over a study period.

- **Keep in mind**

- PW and AW analysis are equivalent
- An alternative has  $AW \geq 0$  if and only if  $PW \geq 0$ .
- An alternative has largest AW among a set of alternatives if and only if it has the largest PW.

- **Capital Recovery (CR) calculation**

- Capital Recovery (CR) is the annualized equivalent of the initial investment  $P$  and salvage value  $S$  of an alternative,

$$CR = -P(A/P, i, n) + S(A/F, i, n) .$$

- Commonly, CR is added to the annual operating costs (AOC) to get AW,

$$AW = CR + AOC .$$

- **Annual worth analysis of permanent investments ( $n = \infty$ )**

- This is similar to the capitalized cost analysis in Chapter 5.
- For a cash flow  $R$ , recurring every  $n_R$  years, starting Year  $n_R$ ,

$$A_R = R(A/F, i, n_R) = R \left[ \frac{i}{(1+i)^{n_R} - 1} \right] .$$

- For a non-recurrent cash flow  $C$ , occurring at Year  $n_C$ ,

$$A_C = C(P/F, i, n_C)(A/P, i, \infty) = \frac{Ci}{(1+i)^{n_C}} .$$